In the context of pg 43 of my lecture notes, show that:

$$\int_{\mathcal{R}} \left[\bigcup_{\varepsilon} \left(\zeta \right) \hat{A} \left(q_{\varepsilon}(\zeta_{1}) \right) \right] =
\int_{\mathcal{R}} q_{\varepsilon} e^{-\frac{1}{\mathcal{R}} S_{\varepsilon} \left[q_{\varepsilon} \right)} A \left(q_{\varepsilon}(\zeta_{1}) \right)$$